

The macroeconomic effects of longevity risk under private and public insurance and asymmetric information

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Annuity puzzle

- Annuity puzzle: despite the theoretical attractiveness of annuities, in practice people tend not to invest much of their wealth in private annuity markets.
- Possible explanations:
 - ▶ Bequest motive
 - ▶ Psychological factors
 - ▶ **Crowding out by social annuities**
 - ▶ **Actuarially unfair rates of return**
 - ★ Administrative costs and taxes
 - ★ Imperfect competition
 - ★ **Adverse selection**
- Goal of the paper: analyze the macroeconomic and welfare effects of adverse selection in private annuity markets and the role of social annuities
- General equilibrium framework instead of partial equilibrium
- Individuals are heterogeneous along two dimensions: health and ability

Main findings

- As in Heijdra & Reijnders (2009): Under asymmetric information there will be a pooling equilibrium in the private annuity market. [Contrast to Bester (1985) and Rothschild & Stiglitz (1976) who argue that credit and insurance markets have separating equilibria.]
- Asymmetric information is important quantitatively (crowding out)
- Funded social security systems cause additional crowding out
- As in Abel (1986), Walliser (2000) and Palmon & Spivak (2007): The introduction of social annuities aggravates adverse selection in the private annuity market
- Even though a social security system is immune to adverse selection, it may decrease welfare
- Privatizing (abolishing) social security is not Pareto improving to all cohorts: shock-time healthy lose out

Outline

1 Model

- Consumers
- Demography
- Firms
- Capital stock dynamics

2 Private annuity markets

- Separating equilibrium
- Pooling equilibrium

3 Public annuities

- Pension system A
- Pension system B
- Pension system C
- Privatizing social security?

Individuals (1)

- Consumers differ in two dimensions:
 - ▶ health (survival probability): μ
 - ▶ ability (labour productivity): η
 - ▶ positive correlation between μ and η
- They live for a maximum of two periods (youth and old age), and work full time during youth and part time during old-age
- Expected lifetime utility of a consumer of type (μ, η) :

$$\mathbb{E}\Lambda_t(\mu, \eta) \equiv U(C_t^y(\mu, \eta)) + \mu\beta U(C_{t+1}^o(\mu, \eta))$$

with:

$$U(x) \equiv \begin{cases} \frac{x^{1-1/\sigma} - 1}{1 - 1/\sigma}, & \text{for } \sigma \neq 1, \\ \ln x & \text{for } \sigma = 1, \end{cases}$$

- ▶ $C_t^y(\mu, \eta)$ is youth-consumption
- ▶ $C_{t+1}^o(\mu, \eta)$ is old-age consumption
- ▶ β is the discount factor due to time preference

Individuals (2)

- Periodic budget constraints:

$$C_t^y(\mu, \eta) + A_t^p(\mu, \eta) = w_t(\eta)$$

$$C_{t+1}^o(\mu, \eta) = \lambda w_{t+1}(\eta) + (1 + r_{t+1}^p(\mu))A_t^p(\mu, \eta)$$

- ▶ $A_t^p(\mu, \eta)$ is annuity purchases
 - ▶ $r_{t+1}^p(\mu)$ is the net rate of return on annuities
 - ▶ $w_t(\eta)$ is the wage rate
 - ▶ λ is the proportion of time devoted to work in old age (exogenous)
- Interior solutions for $C_t^y(\mu, \eta)$ and $A_t^p(\mu, \eta)$:

$$C_t^y(\mu, \eta) = \Phi(\mu, 1 + r_{t+1}^p(\mu)) \left[w_t(\eta) + \frac{\lambda w_{t+1}(\eta)}{1 + r_{t+1}^p(\mu)} \right]$$

$$A_t^p(\mu, \eta) = [1 - \Phi(\mu, 1 + r_{t+1}^p(\mu))] w_t(\eta) - \Phi(\mu, 1 + r_{t+1}^p(\mu)) \frac{\lambda w_{t+1}(\eta)}{1 + r_{t+1}^p(\mu)}$$

with $\Phi(\mu, x) \equiv [1 + (\mu\beta)^\sigma x^{\sigma-1}]^{-1}$

Demography

- The density of consumers with health type μ and working ability η is:

$$L_t(\mu, \eta) \equiv h(\mu, \eta)L_t$$

- ▶ L_t is the size of the population cohort born at time t
- ▶ $h(\mu, \eta)$ is the density function
- The density of (young and old) consumers of type μ alive at time t is:

$$P_t(\mu) \equiv \mu \int_{\eta_L}^{\eta_H} L_{t-1}(\mu, \eta) d\eta + \int_{\eta_L}^{\eta_H} L_t(\mu, \eta) d\eta = \mu h_\mu(\mu) L_{t-1} + h_\mu(\mu) L_t$$

- ▶ $h_\mu(\mu)$ is the marginal distribution of μ
- The newborn cohort sizes evolves according to $L_t = (1 + n)L_{t-1}$ so the total population at time t is:

$$P_t \equiv \int_{\mu_L}^{\mu_H} P_t(\mu) d\mu = \frac{1 + n + \bar{\mu}}{1 + n} L_t$$

- ▶ $\bar{\mu} \equiv \int_{\mu_L}^{\mu_H} \mu h_\mu(\mu) d\mu$ is the average survival rate of a newborn cohort

Production (1)

- Closed economy with perfectly competitive firms
- Production technology is Cobb-Douglas:

$$Y_t = \Omega_0 K_t^\varepsilon N_t^{1-\varepsilon}, \quad 0 < \varepsilon < 1, \quad \Omega_0 > 0$$

- ▶ Y_t is total production
- ▶ K_t is the aggregate capital stock
- ▶ N_t is the *effective* labor force:

$$N_t \equiv \int_{\eta_L}^{\eta_H} \int_{\mu_L}^{\mu_H} \eta [L_t(\mu, \eta) + \lambda L_{t-1}(\mu, \eta)] d\mu d\eta$$

- ▶ N_t has the dimension of worker efficiency (denoted by η) times number of working hours
- ▶ N_t/L_t can be written as:

$$\frac{N_t}{L_t} = \bar{\eta} + \frac{\lambda}{1+n} [\bar{\eta}\bar{\mu} + \text{cov}(\eta, \mu)]$$

where $\text{cov}(\eta, \mu)$ is the (positive) covariance between μ and η

Production (2)

- Intensive-form production function:

$$y_t = \Omega_0 k_t^\varepsilon$$

with $y_t \equiv Y_t/N_t$ and $k_t \equiv K_t/N_t$

- Factor demand equations:

$$r_t + \delta = \varepsilon \Omega_0 k_t^{\varepsilon-1}$$

$$w_t = (1 - \varepsilon) \Omega_0 k_t^\varepsilon$$

$$w_t(\eta) = \eta w_t$$

- ▶ r_t is the net rate of return on physical capital
- ▶ δ is the depreciation rate of capital ($0 < \delta < 1$)
- ▶ w_t is the rental rate on efficiency units of labour

Equilibrium

- Capital market clearing condition:

$$K_{t+1} = L_t \int_{\mu_L}^{\mu_H} \int_{\eta_L}^{\eta_H} A_t^P(\mu, \eta) h(\mu, \eta) d\eta d\mu \quad (\text{FDE})$$

- The demand for annuities $A_t^P(\mu, \eta)$ depends on w_t , w_{t+1} , and $r_{t+1}^P(\mu)$
- The rate of return on annuities $r_{t+1}^P(\mu)$ depends on r_{t+1}
- Hence: w_t and (w_{t+1}, r_{t+1}) depend on, respectively, k_t and k_{t+1} so (FDE) is a non-linear implicit function relating k_{t+1} to k_t and the exogenous variables

Perfect information in the private annuity market

- Benchmark assumptions:

- (A0) Health status is public information.

- (A1) The annuity market is perfectly competitive. There is a large number of risk neutral firms offering annuities to individuals, and firms can freely enter or exit the market.

- (A2) Annuity firms do not use up any real resources.

- Separating equilibrium

- Zero-profit condition for each μ :

$$(1 + r_{t+1}) \int_{\eta_L}^{\eta_H} L_t(\mu, \eta) A_t^P(\mu, \eta) d\eta = (1 + r_{t+1}^P(\mu)) \int_{\eta_L}^{\eta_H} \mu L_t(\mu, \eta) A_t^P(\mu, \eta) d\eta$$

- Annuity rate of return for μ -type individual:

$$1 + r_{t+1}^P(\mu) = \frac{1 + r_{t+1}}{\mu}$$

- Full annuitization optimal as $r_{t+1}^P(\mu) > r_{t+1}$ for all μ

- Economic intuition: **Figure 2**

▶ show

Parameterization and visualization

- Model too stylized to calibrate on an actual economy
- Parameterization approach
 - ▶ Pick plausible values for σ , δ_a , n_a , and \hat{r}_a
 - ▶ Set length of life period at 40 years
 - ▶ Set mandatory retirement age at 65 years (by choice of λ)
 - ▶ Postulate a joint distribution for μ and η : bivariate uniform with a positive correlation between the two ($\text{cor}(\mu, \eta) = 0.3$). See **Figure 1** [▶ show](#)
- Summary of the structural parameters: **Table 1** [▶ show](#)
- Steady-state equilibrium under **Full Information**: **Table 2(a)** [▶ show](#)
- Steady-state average profiles by health (solid lines): **Figure 3** [▶ show](#)

Asymmetric information in the private annuity market (1)

- Replace Assumption (A0) by:

- (A3) Health status and productivity are private information of the annuitant. The distribution of health and productivity types in the population, $H(\mu, \eta)$, is common knowledge.
- (A4) Annuitants can buy multiple annuities for different amounts and from different annuity firms. Individual annuity firms cannot monitor their clients' wage income or annuity holdings with other firms.

- Pooling equilibrium

- ▶ Healthy agents ($\mu_t^{bc} \leq \mu \leq \mu_H$) buy annuities and face a common rate, $r_{t+1}^p(\mu) = \bar{r}_{t+1}^p$
- ▶ Unhealthy agents ($\mu_L \leq \mu < \mu_t^{bc}$) drop out of the annuity market and face borrowing constraints

- The zero-profit condition for the private annuity market is given by:

$$(1+r_{t+1}) \int_{\eta_L}^{\eta_H} \int_{\mu_t^{bc}}^{\mu_H} L_t(\mu, \eta) A_t^p(\mu, \eta) d\mu d\eta = (1+\bar{r}_{t+1}^p) \int_{\eta_L}^{\eta_H} \int_{\mu_t^{bc}}^{\mu_H} \mu L_t(\mu, \eta) A_t^p(\mu, \eta) d\mu d\eta$$

Asymmetric information in the private annuity market (2)

- The pooling rate is:

$$1 + \bar{r}_{t+1}^p = \frac{1 + r_{t+1}}{\bar{\mu}_t^p}$$

- Here $\bar{\mu}_t^p$ is the asset-weighted average survival rate of annuity purchasers:

$$\bar{\mu}_t^p \equiv \int_{\mu^{bc}}^{\mu_H} \mu \omega_t(\mu) d\mu, \quad \omega_t(\mu) \equiv \frac{\int_{\eta_L}^{\eta_H} A_t^p(\mu, \eta) h(\mu, \eta) d\eta}{\int_{\eta_L}^{\eta_H} \int_{\mu^{bc}}^{\mu_H} A_t^p(\mu, \eta) h(\mu, \eta) d\mu d\eta}$$

- Since $\mu_t^{bc} < \bar{\mu}_t^p < \mu_H < 1$ it follows that \bar{r}_{t+1}^p exceeds r_{t+1} : all net savers will completely annuitize their wealth
- Economic intuition: **Figure 4**

▶ show

Asymmetric information in the private annuity market (3)

- The pooling rate is demographically unfair because it is based on the *asset-weighted* survival rate $\bar{\mu}_t^P$ rather than on the *average* survival rate in the population $\bar{\mu}$
- The demographically fair pooling rate is given by:

$$1 + \bar{r}_{t+1}^{df} = \frac{1 + r_{t+1}}{\bar{\mu}}$$

and, since $\bar{\mu} < \bar{\mu}_t^P$ it follows readily that $\bar{r}_{t+1}^P < \bar{r}_{t+1}^{df}$

- Steady-state equilibrium under **Asymmetric Information**: **Table 2(b)** [▶ show](#)
- Steady-state average profiles by health (dashed lines): **Figure 3** [▶ show](#)

Fully funded pensions (1)

- Features of the Asymmetric Information equilibrium:
 - ▶ Relatively unhealthy annuitants face a disadvantageous pooling rate of interest on their annuities. In essence such individuals are subsidizing their healthy cohort members through the annuity market.
 - ▶ Very unhealthy individuals drop out of the annuity market and face binding borrowing constraints
- A government-run and fully-funded mandatory social security system is immune to adverse selection because all individuals are forced to participate in it
- Pension contributions during youth
 - ▶ An individual's contributions during youth are proportional to wage income, $A_t^s(\eta) = \theta w_t(\eta)$, where θ is the social security tax (such that $0 < \theta < 1$)
 - ▶ Total pension contributions, $A_t^s = \theta \bar{\eta} w_t L_t$, are invested in the capital market earning a gross rate of return equal to $1 + r_{t+1}$
 - ▶ In the next period the returns $R_{t+1} = (1 + r_{t+1})A_t^s$ are paid out to surviving agents

Fully funded pensions (2)

- Pension receipts during old-age
 - ▶ System A: pension receipts during old-age are proportional to contributions made during youth
 - ▶ System B: pension contributions of η types are distributed during old-age to surviving η types
 - ▶ System C: pension receipts are the same in absolute value for all surviving agents
- What are the allocational and welfare effects of public annuities?

Pension system A (SA_A)

- Pension received by an η individual:

$$R_{t+1}^s(\eta) = \zeta \theta w_t(\eta)$$

- The clearing condition for the public annuity system:

$$(1 + r_{t+1})A_t^s = \int_{\eta_L}^{\eta_H} \int_{\mu_L}^{\mu_H} \mu R_{t+1}^s(\eta) L_t(\mu, \eta) d\mu d\eta$$

- Since $w_t(\eta) = \eta w_t$ the balanced-budget solution for ζ is:

$$\zeta = \zeta_A \frac{1 + r_{t+1}}{\bar{\mu}}, \quad \zeta_A \equiv \frac{\bar{\eta} \bar{\mu}}{\text{cov}(\eta, \mu) + \bar{\eta} \bar{\mu}}$$

- Since $0 < \zeta_A < 1$, the rate of return on social annuities falls short of the demographically fair social annuity yield, $(1 + r_{t+1})/\bar{\mu}$, because health and productivity are positively correlated (high contributors tend to live longer than average)

Pension system A (2)

- Effective pension contribution rate is:

$$\theta_t^n \equiv \theta \left(1 - \zeta_A \frac{\bar{\mu}_t^p}{\bar{\mu}} \right)$$

where the plausible case is that $\theta_t^n < 0$ (see **Figure 9(c)**)

- Economic intuition: **Figure 5**
- Steady-state equilibrium under SA_A : **Table 2(c)-(d)**
- Comparison SA_A (solid lines) and AI (dashed lines) in **Figure 6**

▶ show

▶ show

▶ show

▶ show

Pension system B (SA_B)

- The pension authority uses its knowledge of η by setting pension receipts according to the following rule:

$$R_{t+1}^s(\eta) = \zeta(\eta)\theta w_t(\eta)$$

- The clearing condition for the public annuity system:

$$(1 + r_{t+1})\theta w_t(\eta) \int_{\mu_L}^{\mu_H} L_t(\mu, \eta) d\mu = \int_{\mu_L}^{\mu_H} \mu R_{t+1}^s(\eta) L_t(\mu, \eta) d\mu$$

- Since $w_t(\eta) = \eta w_t$ the balanced-budget solution for $\zeta(\eta)$ is:

$$\zeta(\eta) = \zeta_B(\eta) \frac{1 + r_{t+1}}{\bar{\mu}}, \quad \zeta_B(\eta) \equiv \frac{\bar{\mu}}{\bar{\mu} + \xi \sigma_{\mu}^2 (\eta - \bar{\eta})} \begin{matrix} > \\ = \\ < \end{matrix} 1 \Leftrightarrow \eta \begin{matrix} < \\ = \\ > \end{matrix} \bar{\eta}$$

- *Explicit* redistribution from high-ability to low-ability individuals
- *Implicit* redistribution from healthy to unhealthy individuals (due to positive correlation between ability and health)

Pension system B (2)

- Effective pension contribution rate is:

$$\theta_t^n(\eta) \equiv \theta \left(1 - \zeta_B(\eta) \frac{\bar{\mu}_t^P}{\bar{\mu}} \right)$$

where the plausible case is that $\theta_t^n(\eta) < 0$ for all η (see **Figure 9(c)**)

- Economic intuition: **Figure 7**
- Steady-state equilibrium under SA_B : **Table 2(e)**
- Comparison SA_B (solid lines) and AI (dashed lines) in **Figure 10**

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▶ show

▶ show

▶ show

Pension system C (SA_C)

- The pension authority provides everybody with the same pension:

$$R_{t+1}^s(\eta) = \bar{R}_{t+1}^s$$

- The clearing condition for the public annuity system:

$$(1 + r_{t+1})\theta\bar{\eta}w_tL_t = L_t \int_{\mu_L}^{\mu_H} \int_{\eta_L}^{\eta_H} \mu \bar{R}_{t+1}^s h(\mu, \eta) d\eta d\mu \quad \Leftrightarrow$$
$$\bar{R}_{t+1}^s = \theta\bar{\eta}w_t \frac{1 + r_{t+1}}{\bar{\mu}}$$

- In summary:

$$R_{t+1}^s(\eta) = \zeta(\eta)\theta w_t(\eta)$$

$$\zeta(\eta) = \zeta_C(\eta) \frac{1 + r_{t+1}}{\bar{\mu}}, \quad \zeta_C(\eta) \equiv \frac{\bar{\eta}}{\eta} \begin{matrix} > \\ = \\ < \end{matrix} 1 \Leftrightarrow \eta \begin{matrix} < \\ = \\ > \end{matrix} \bar{\eta}$$

- Redistribution is similar to that under pension system B

Pension system C (2)

- Effective pension contribution rate is:

$$\theta_t^n(\eta) \equiv \theta \left(1 - \zeta_C(\eta) \frac{\bar{\mu}_t^P}{\bar{\mu}} \right)$$

where the plausible case is that $\theta_t^n(\eta) > 0$ for very high value of η (see **Figure 9(c)**)

- Steady-state equilibrium under SA_C : **Table 2(g)**
- Comparison SA_C (solid lines) and AI (dashed lines) in **Figure 11**

▶ show

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Summary on public annuities

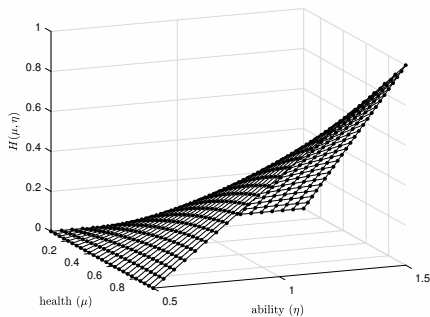
- All pension systems that we have studied are immune to adverse selection by design but they:
 - ▶ exacerbate the adverse selection problem in the market for private annuities
 - ▶ increase the fraction of borrowing-constrained ('over-annuitized') individuals in the population. See **Figure 8** [▶ show](#)
 - ▶ lead to long-run crowding out of capital and substantial output losses. See **Table 2** [▶ show](#)
- Is it better to privatize social security altogether and to allow individuals to insure against longevity risk in the private annuity market even though this market is not perfect?
- Privatising social security: Abolishing pension system A
 - ▶ Large steady-state output and welfare gains
 - ▶ There is some transitional dynamics in macro variables. See **Figure 12** [▶ show](#)
 - ▶ Privatization is not a 'win-win' scenario. Shock-time healthy individuals are worse off as a result of the privatization. See **Figure 13** [▶ show](#)

Conclusions

- When an individual's health and ability are private information there will be a pooling equilibrium in the private annuity market
- Asymmetric information matters quantitatively
- Funded social security causes further crowding out under asymmetric information
- When people differ along two dimensions (health and ability) private and public longevity insurance cause explicit and implicit redistribution effects
- Pension systems that redistribute from high- to low-ability types exacerbate the incidence of borrowing constraints
- Abolishing social security does not benefit all cohorts

Figure 1: Features of the distribution for μ and η

(a) Distribution
 $H(\mu, \eta)$



(b) Density
 $h(\mu, \eta)$

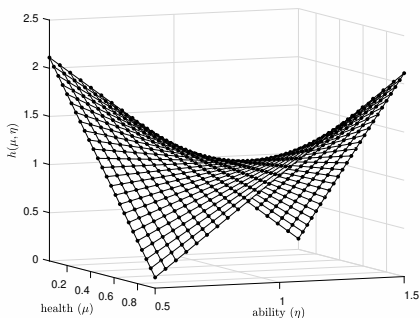


Figure 2: Consumption-saving choices under full information

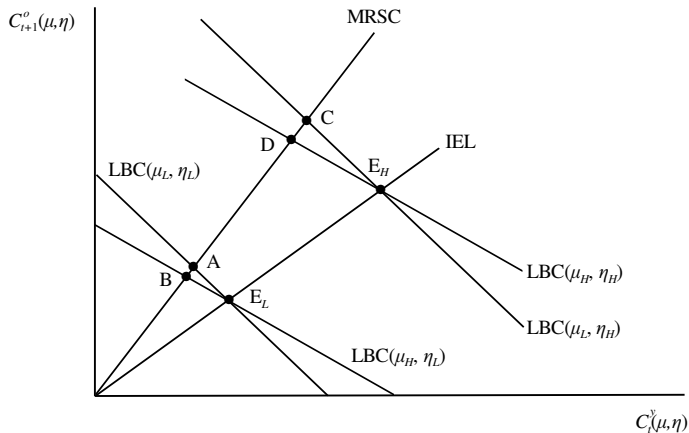
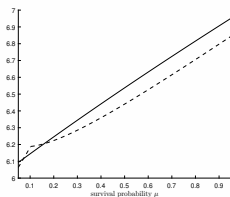
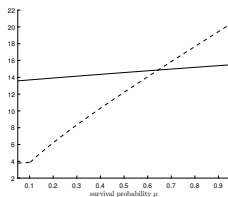


Figure 3: Steady-state profiles

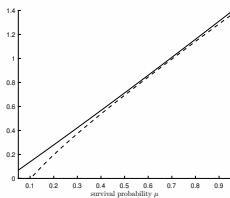
(a) Youth consumption
 $\hat{C}^y(\mu)$



(b) Old-age consumption
 $\hat{C}^o(\mu)$



(c) Annuity demand
 $\hat{A}^p(\mu)$



(d) Expected utility
 $\mathbb{E}\hat{\Lambda}(\mu)$

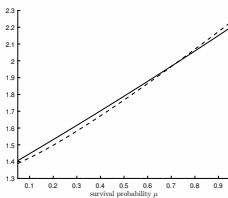
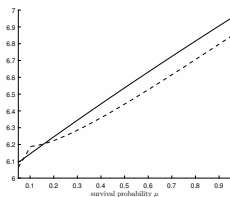
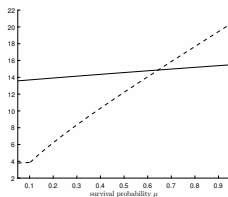


Figure 3: Steady-state profiles

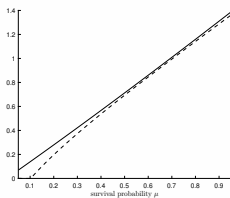
(a) Youth consumption
 $\hat{C}^y(\mu)$



(b) Old-age consumption
 $\hat{C}^o(\mu)$



(c) Annuity demand
 $\hat{A}^p(\mu)$



(d) Expected utility
 $\mathbb{E}\hat{\Lambda}(\mu)$

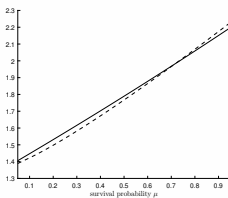


Figure 4: Consumption-saving choices under asymmetric information

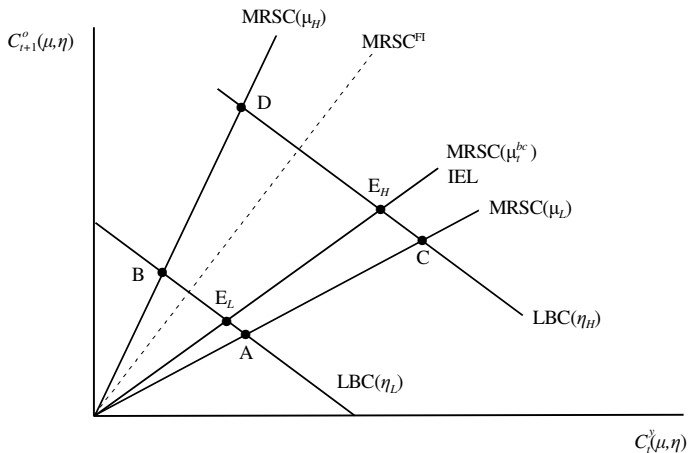


Figure 5: Consumption-saving choices under pension system A

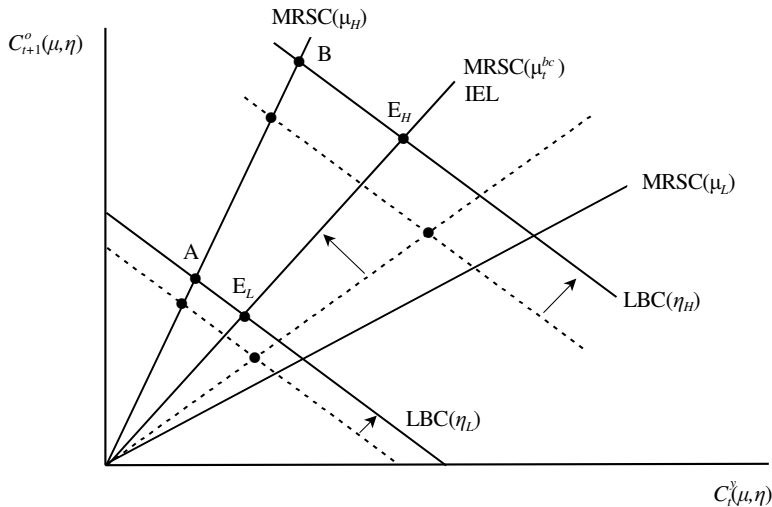
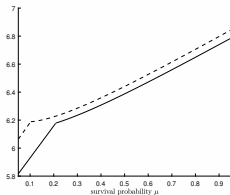
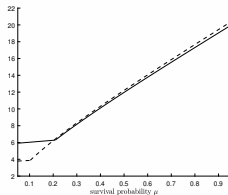


Figure 6: Steady-state profiles under pension system A

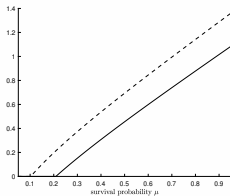
(a) Youth consumption
 $\hat{C}^y(\mu)$



(b) Old-age consumption
 $\hat{C}^o(\mu)$



(c) Annuity demand
 $\hat{A}^p(\mu)$



(d) Expected utility
 $\mathbb{E}\hat{\Lambda}(\mu)$

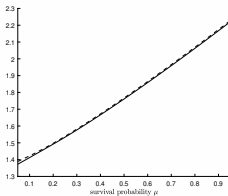


Figure 7: Consumption-saving choices under pension system B

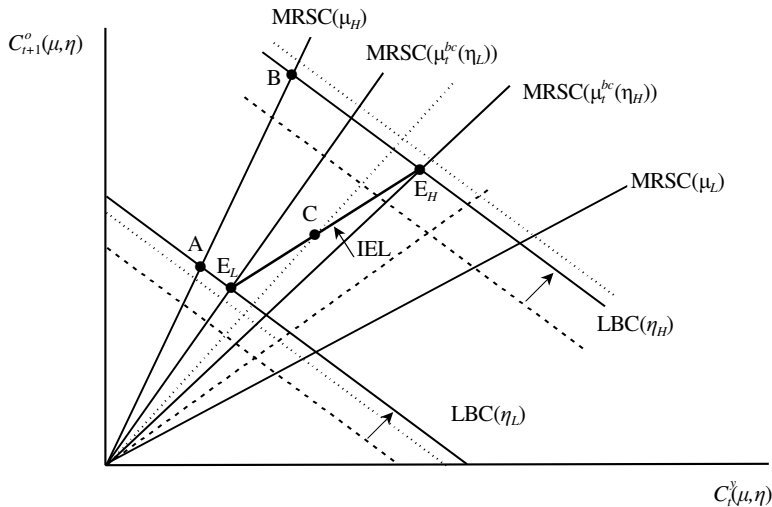


Figure 8: Ability and borrowing constraints

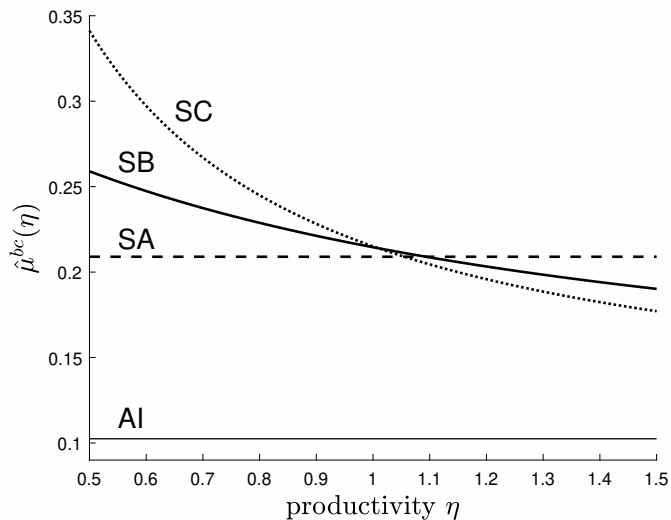
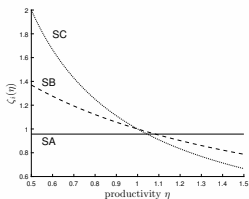


Figure 9: Comparing pension systems

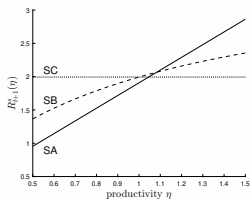
(a) Fair-rate share

$$\zeta_i(\eta)$$



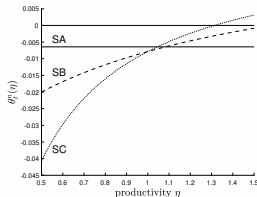
(b) Pension receipt

$$R_{t+1}^s(\eta)$$



(c) Effective pension contribution rate

$$\theta_t^n(\eta)$$



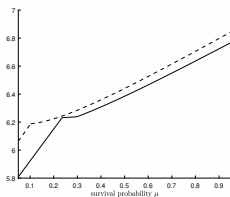
▶ return to SA_A

▶ return to SA_B

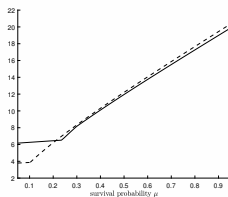
▶ return to SA_C

Figure 10: Steady-state profiles under pension system B

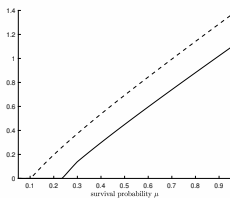
(a) Youth consumption
 $\hat{C}^y(\mu)$



(b) Old-age consumption
 $\hat{C}^o(\mu)$



(c) Annuity demand
 $\hat{A}^P(\mu)$



(d) Expected utility
 $\mathbb{E}\hat{\Lambda}(\mu)$

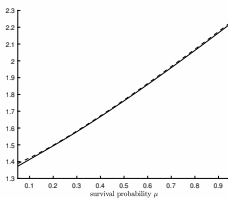
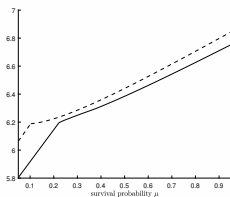
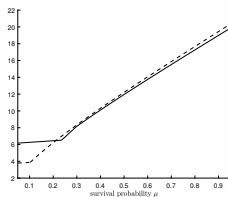


Figure 11: Steady-state profiles under pension system C

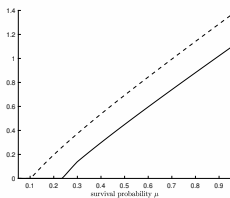
(a) Youth consumption
 $\hat{C}^y(\mu)$



(b) Old-age consumption
 $\hat{C}^o(\mu)$



(c) Annuity demand
 $\hat{A}^P(\mu)$



(d) Expected utility
 $\mathbb{E}\hat{\Lambda}(\mu)$

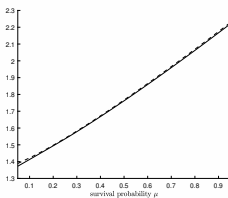
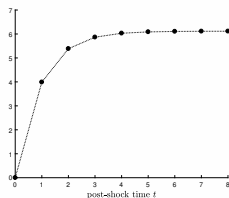


Figure 12: Abolishing pension system A

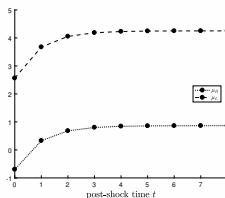
(a) Capital intensity

$$\frac{\Delta k_t}{\hat{k}} \cdot 100\%$$



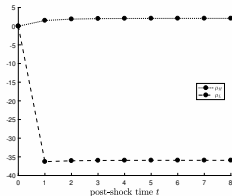
(b) Youth consumption

$$\frac{\Delta C_t^o(\mu_i, \eta_L)}{\hat{C}^o(\mu_i, \eta_L)} \cdot 100\%$$



(c) Old-age consumption

$$\frac{\Delta C_t^y(\mu_i, \eta_L)}{\hat{C}^y(\mu_i, \eta_L)} \cdot 100\%$$



(d) Annuity demand

$$\frac{\Delta A_t^p(\mu_i, \eta_L)}{\hat{A}^p(\mu_i, \eta_L)} \cdot 100\%$$

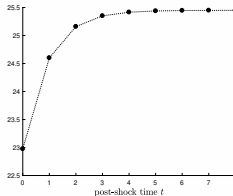
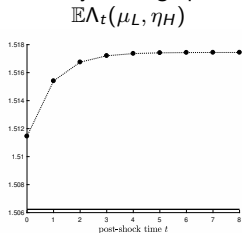
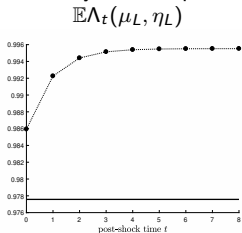


Figure 13: Lifetime utility of corner types

(a) Unhealthy and low productivity (b) Unhealthy and high productivity



(c) Healthy and low productivity (d) Healthy and high productivity

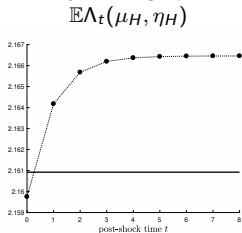
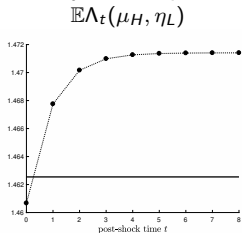


Table 1: Structural parameters

σ	intertemporal substitution elasticity		0.7000
ε	capital efficiency parameter		0.2750
δ_a	annual capital depreciation rate		0.0600
δ	capital depreciation factor		0.9158
n_a	population growth rate		0.0100
n	population growth factor		0.4889
β	time preference parameter	c	0.4462
λ	mandatory retirement parameter		0.6250
Ω_0	scale factor production function	c	12.9071
μ_L	survival rate of the unhealthiest		0.0500
μ_H	survival rate of the healthiest		0.9500
η_L	lowest working ability		0.5000
η_H	highest working ability		1.5000
ξ	covariance parameter of the distribution function		4.0000

Table 2: Allocation and welfare

	(a) FI	(b) AI	(c) SA _A $\theta = 0.010$	(d) SA _A $\theta = 0.025$	(e) SA _B $\theta = 0.010$	(f) SA _B $\theta = 0.025$	(g) SA _C $\theta = 0.010$	(h) SA _C $\theta = 0.025$
\hat{y}	10.000	9.840	9.776	9.680	9.768	9.668	9.762	9.660
\hat{k}	0.395	0.373	0.364	0.351	0.363	0.350	0.362	0.349
%Q1	12.34	11.78	10.15	7.73	9.69	6.69	9.15	5.50
%Q2	19.81	19.46	17.14	13.59	16.90	12.98	16.75	12.60
%Q3	28.73	28.84	25.81	21.05	25.92	21.26	26.12	21.66
%Q4	39.12	39.93	36.18	30.11	36.74	31.46	37.22	32.58
%SAS			10.72	27.51	10.74	27.60	10.76	27.67
\hat{r}	6.04	6.34	6.47	6.66	6.48	6.69	6.50	6.70
\hat{r}^a	5.00%	5.11%	5.16%	5.22%	5.16%	5.23%	5.17%	5.24%
\hat{w}	7.250	7.134	7.087	7.018	7.082	7.010	7.077	7.003
\widehat{BC}	0.00%	5.83%	10.03%	17.66%	10.63%	19.33%	10.63%	19.33%
$\hat{p}P$		10.18	10.12	9.99	10.12	9.98	10.12	9.96
$\hat{\mu}P$		0.66	0.67	0.70	0.67	0.70	0.67	0.70
\widehat{AS}		1.31	1.34	1.39	1.35	1.40	1.35	1.41
$\hat{\varepsilon}^Y$	5.357	5.296	5.270	5.233	5.268	5.228	5.265	5.225
%Q1	15.99	16.03	16.02	15.98	16.06	16.09	16.12	16.20
%Q2	22.10	22.13	22.12	22.10	22.14	22.16	22.16	22.20
%Q3	28.06	28.05	28.05	28.06	28.04	28.04	28.02	27.99
%Q4	33.85	33.79	33.81	33.86	33.75	33.72	33.70	33.61
$\hat{\varepsilon}^O$	4.087	4.021	3.994	3.954	3.991	3.949	3.988	3.946
%Q1	12.23	10.70	10.72	10.77	10.77	10.93	10.83	11.14
%Q2	19.74	18.78	18.79	18.82	18.82	18.90	18.83	18.95
%Q3	28.75	29.04	29.03	29.02	29.02	28.98	29.00	28.91
%Q4	39.28	41.48	41.46	41.39	41.39	41.18	41.33	41.00
$E\hat{\Lambda}(\mu_L, \eta_L)$	1.014	0.996	0.989	0.978	1.022	1.020	1.026	1.029
$E\hat{\Lambda}(\mu_H, \eta_L)$	1.433	1.471	1.468	1.463	1.260	1.261	1.266	1.276
$E\hat{\Lambda}(\mu_L, \eta_H)$	1.529	1.517	1.513	1.506	1.532	1.527	1.531	1.525
$E\hat{\Lambda}(\mu_H, \eta_H)$	2.143	2.167	2.164	2.161	2.031	2.026	2.030	2.024

Table 2: Allocation and welfare

	(a) FI	(b) AI	(c) SA _A $\theta = 0.010$	(d) SA _A $\theta = 0.025$	(e) SA _B $\theta = 0.010$	(f) SA _B $\theta = 0.025$	(g) SA _C $\theta = 0.010$	(h) SA _C $\theta = 0.025$
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\hat{k}	0.395	0.373	0.364	0.351	0.363	0.350	0.362	0.349
%Q1	12.34	11.78	10.15	7.73	9.69	6.69	9.15	5.50
%Q2	19.81	19.46	17.14	13.59	16.90	12.98	16.75	12.60
%Q3	28.73	28.84	25.81	21.05	25.92	21.26	26.12	21.66
%Q4	39.12	39.93	36.18	30.11	36.74	31.46	37.22	32.58
%SAS			10.72	27.51	10.74	27.60	10.76	27.67
\hat{r}	6.04	6.34	6.47	6.66	6.48	6.69	6.50	6.70
\hat{r}^a	5.00%	5.11%	5.16%	5.22%	5.16%	5.23%	5.17%	5.24%
\hat{w}	7.250	7.134	7.087	7.018	7.082	7.010	7.077	7.003
\widehat{BC}	0.00%	5.83%	10.03%	17.66%	10.63%	19.33%	10.63%	19.33%
$\hat{p}P$		10.18	10.12	9.99	10.12	9.98	10.12	9.96
$\hat{\mu}P$		0.66	0.67	0.70	0.67	0.70	0.67	0.70
\widehat{AS}		1.31	1.34	1.39	1.35	1.40	1.35	1.41
$\hat{\varepsilon}^Y$	5.357	5.296	5.270	5.233	5.268	5.228	5.265	5.225
%Q1	15.99	16.03	16.02	15.98	16.06	16.09	16.12	16.20
%Q2	22.10	22.13	22.12	22.10	22.14	22.16	22.16	22.20
%Q3	28.06	28.05	28.05	28.06	28.04	28.04	28.02	27.99
%Q4	33.85	33.79	33.81	33.86	33.75	33.72	33.70	33.61
$\hat{\varepsilon}^O$	4.087	4.021	3.994	3.954	3.991	3.949	3.988	3.946
%Q1	12.23	10.70	10.72	10.77	10.77	10.93	10.83	11.14
%Q2	19.74	18.78	18.79	18.82	18.82	18.90	18.83	18.95
%Q3	28.75	29.04	29.03	29.02	29.02	28.98	29.00	28.91
%Q4	39.28	41.48	41.46	41.39	41.39	41.18	41.33	41.00
$E\hat{\Lambda}(\mu_L, \eta_L)$	1.014	0.996	0.989	0.978	1.022	1.020	1.026	1.029
$E\hat{\Lambda}(\mu_H, \eta_L)$	1.433	1.471	1.468	1.463	1.260	1.261	1.266	1.276
$E\hat{\Lambda}(\mu_L, \eta_H)$	1.529	1.517	1.513	1.506	1.532	1.527	1.531	1.525
$E\hat{\Lambda}(\mu_H, \eta_H)$	2.143	2.167	2.164	2.161	2.031	2.026	2.030	2.024

Table 2: Allocation and welfare

	(a) FI	(b) AI	(c) SA _A $\theta = 0.010$	(d) SA _A $\theta = 0.025$	(e) SA _B $\theta = 0.010$	(f) SA _B $\theta = 0.025$	(g) SA _C $\theta = 0.010$	(h) SA _C $\theta = 0.025$
\hat{y}	10.000	9.840	9.776	9.680	9.768	9.668	9.762	9.660
\hat{k}	0.395	0.373	0.364	0.351	0.363	0.350	0.362	0.349
%Q1	12.34	11.78	10.15	7.73	9.69	6.69	9.15	5.50
%Q2	19.81	19.46	17.14	13.59	16.90	12.98	16.75	12.60
%Q3	28.73	28.84	25.81	21.05	25.92	21.26	26.12	21.66
%Q4	39.12	39.93	36.18	30.11	36.74	31.46	37.22	32.58
%SAS			10.72	27.51	10.74	27.60	10.76	27.67
\hat{r}	6.04	6.34	6.47	6.66	6.48	6.69	6.50	6.70
\hat{r}^a	5.00%	5.11%	5.16%	5.22%	5.16%	5.23%	5.17%	5.24%
\hat{w}	7.250	7.134	7.087	7.018	7.082	7.010	7.077	7.003
\widehat{BC}	0.00%	5.83%	10.03%	17.66%	10.63%	19.33%	10.63%	19.33%
$\hat{p}P$		10.18	10.12	9.99	10.12	9.98	10.12	9.96
$\hat{\mu}P$		0.66	0.67	0.70	0.67	0.70	0.67	0.70
\widehat{AS}		1.31	1.34	1.39	1.35	1.40	1.35	1.41
$\hat{\varepsilon}^Y$	5.357	5.296	5.270	5.233	5.268	5.228	5.265	5.225
%Q1	15.99	16.03	16.02	15.98	16.06	16.09	16.12	16.20
%Q2	22.10	22.13	22.12	22.10	22.14	22.16	22.16	22.20
%Q3	28.06	28.05	28.05	28.06	28.04	28.04	28.02	27.99
%Q4	33.85	33.79	33.81	33.86	33.75	33.72	33.70	33.61
$\hat{\varepsilon}^O$	4.087	4.021	3.994	3.954	3.991	3.949	3.988	3.946
%Q1	12.23	10.70	10.72	10.77	10.77	10.93	10.83	11.14
%Q2	19.74	18.78	18.79	18.82	18.82	18.90	18.83	18.95
%Q3	28.75	29.04	29.03	29.02	29.02	28.98	29.00	28.91
%Q4	39.28	41.48	41.46	41.39	41.39	41.18	41.33	41.00
$E\hat{\Lambda}(\mu_L, \eta_L)$	1.014	0.996	0.989	0.978	1.022	1.020	1.026	1.029
$E\hat{\Lambda}(\mu_H, \eta_L)$	1.433	1.471	1.468	1.463	1.260	1.261	1.266	1.276
$E\hat{\Lambda}(\mu_L, \eta_H)$	1.529	1.517	1.513	1.506	1.532	1.527	1.531	1.525
$E\hat{\Lambda}(\mu_H, \eta_H)$	2.143	2.167	2.164	2.161	2.031	2.026	2.030	2.024